

## INDIVIDUAL ASSIGNMENT 2

(**due:** Problem 1: Wednesday **Jan. 24**; Problem 2:<sup>1</sup> Monday **Jan. 29**, both **before class** )

- This is **not** a programming assignment. For this individual assignment prepare a *concise* (and readable) answer sheet and hand it on the due date, just **before class**. Write your **name** and **email** address on the front page.

**Problem 1 (Types, Function Signatures)** Below the function signatures are in the style of Haskell type declarations.

- a) Explain the type of each of the expressions  $f_1$ ,  $f_2$ , and  $f_3$ :

```
f1 :: String -> Integer
f2 :: Integer -> String
f3 :: (Integer, String) -> Bool
```

Let's assume the *domain* of each  $f_i$  is *finite*. What other names (from the class) describe best the type of each  $f_i$ ?

- b) Explain the function signatures for

```
f :: a -> (b -> c)
g :: (a -> b) -> c -> d
```

Hint: e.g., for  $f$  think of integer addition, i.e., let  $a = b = c = \text{Integer}$ . What are the values and types say for  $f\ 17\ 3$  and  $f\ 17$  if  $f$  denotes integer addition.

For  $g$ , think of the `map` function explained in class. What types make sense for  $c$  and  $d$  in case of the `map` function?

**Problem 2 (Functions vs Relations)** “ $(A \rightarrow B)$ ” is the *set of all functions* from  $A$  to  $B$ . “ $(A \times B)$ ” is the *Cartesian product* of  $A$  and  $B$ . Let  $A = \{1, 2, \dots, n\}$  and  $B = \{1, 2, \dots, m\}$

- a) How many elements has “ $(A \times B)$ ”?
- b) How many elements has “ $(A \rightarrow B)$ ”?
- c) Let  $k$  be given. How can we model a relation over  $A_1, \dots, A_k$  as a function? (Hint: it is sufficient to give a Haskell signature)

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<sup>1</sup>But preferably you should turn in Problem 2 together with Problem 1, since there will be a programming assignment coming out on Wednesday!